Graph-Theoretic Methods

Homework #1 (2012-2013)

Q1: What is the sum of the eigenvalues of the graph Laplacian?

Q2: Recall that the vertex incidence matrix Q of a graph, a rectangular matrix with a row for each edge and a column for each vertex that has the property that  $L = Q^T Q$ .  $QQ^T$  is a matrix that has the same eigenvalues as L. Provide an interpretation for  $QQ^T - 2I$ .